

## Performance analysis of differentiated QoS in IEEE 802.11e WLANs<sup>¶</sup>

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### SUMMARY

This paper proposes a multi-dimensional Markov model to analyse the performance of the IEEE 802.11e EDCF MAC protocol. Based on this model, we present extensive performance evaluation in terms of throughput, throughput ratios, and access delay of flows of distinct priorities under RTS/CTS mode. We also provide quantitative analysis of the impact of prioritized parameters, i.e. Arbitration InterFrame Space (AIFS), Contention Window (CW) on Quality of Service (QoS) differentiation. The accuracy of the proposed model is verified by means of comparing the numerical results obtained from both analytical model and simulations. Our research can be used as a guideline for the prediction of how flows belonging to a certain Traffic Category (TC) perform with their TC-specific parameters, as well as designing EDCF-based WLANs and tuning the parameters to achieve the desirable differentiated QoS objectives. Copyright © 2005 John Wiley & Sons, Ltd.

KEY WORDS: Quality of service (QoS); service differentiation; MAC; IEEE802.11e; EDCF; WLANs; Markov chain

### 1. INTRODUCTION

The Enhanced Distributed Coordination Function (EDCF) is a Quality of Service (QoS)-enabled multiple access scheme defined by IEEE802.11E standard draft [1]. It is a fully distributed, CSMA/CA-based MAC algorithm, but provides access to the Wireless Media (WM) with up to eight priorities, also known as Traffic Categories (TCs). The differentiated access is achieved by having each QoS station (QSTA) operate maximum eight output queues, which are called Virtual Stations (VSs); each VS independently contends for channel access.

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formulation for throughput and delay. In Section 4, we validate the results of our model by comparing with simulation results. In Section 5, we carry out the performance evaluation, with insights of how much the parameters of EDCF impact differentiation QoS to different TCs. Finally, in Section 6, we conclude the paper.

## 2. RELATED WORK AND MOTIVATION

Besides EDCF specified by task group E, there are other efforts to enhance the CSMA/CA access scheme to provide QoS. Research in References [2–15] has revealed that, based on CSMA/CA access scheme, packet-level QoS can be achieved by differentiating the operation parameters of STAs, enhancing the CW algorithm and separating traffic flows. MACAW in Reference [2] was one of an early MAC protocol intended to provide QoS, particularly per flow fairness. Among other mechanisms, multiplicative increase/linear decrease (MILD) CW algorithms, ‘backoff copy’, and per-flow CW paradigm were proposed to provide better fair access to packet streams across multiple cells.

In Reference [3], efficient channel utilization and weighted fairness were achieved by dynamically selecting the proper CW to reflect the relative weights among data traffic flows and the number of the stations contending for the wireless medium. Therefore, the window size has to be calculated based on the network traffic condition, which is monitored and tracked down along with the operation. The work in Reference [4] took the similar approach to achieving per-flow fair medium access.

In References [5, 6], balanced media access methods (BMAM) was proposed to provide per-flow fair transmission. BMAM introduced the concept of persistence factor, say  $p$ , as the leverage of fairness, which is similar to  $p$ -persistence CSMA. In BMAM, stations send packets with probability  $p$ , after the backoff period, or back off again with probability  $1 - p$  using the same CW value, where  $p$  can be calculated dynamically using either contention- or time-based media access method, in order to achieve fairness objective.

In Reference [7], a general analytical framework was introduced to model system wide per-flow fairness via the specification of per-flow utility functions. Then the fairness model could be translated into a corresponding contention resolution algorithm. Using this translation, the backoff algorithm for achieving proportional fairness was derived.

The work in References [8, 9] presented a set of cooperative mechanisms that compose a fully distributed wireless differentiated services network. Among others, a distributed, differentiated services-capable MAC was described. The protocol is a modification of DCF in IEEE802.11 and data transmission follows the same listen-before-talk scheme. However, best effort and premium traffic streams use the different CW bounds so that premium traffic tends to wait shorter than the best effort traffic before initiating data exchange sequence. The work in Reference [10] takes the similar approach to enabling QoS in MAC layer.

In Reference [11], three DCF factors, namely, CW size, interframe spaces and packet lengths were studied as the leverage of service differentiation. The authors simulated and compared the delay and bandwidth of prioritized flows when using one of three differentiation mechanisms. Firstly, each priority level has a different backoff increment function. Secondly, each priority level is assigned a different DIFS length. And lastly, each priority level has a different maximum frame length, beyond which the frame has to be segmented and transmitted multiple times.

Similarly, Reference [12] proposed and evaluated different CW algorithms for the prioritized flows.

The work in References [13,14] attempted to achieve weighted fairness of flows with distributed control, which is facilitated by transmission status information exchange. The scheme introduced in Reference [13] tries to mimic the centralized Self-Clocked Fair Queuing (SCFQ) algorithm using the piggybacked timer information and selecting backoff intervals proportional to normalized packet sizes by flow weights, i.e. packet size/weight. Paper [14] chose a CW size proportional to normalized rate of each flow.

In terms of EDCF performance on QoS support, we are on the very early stage of research. A few research efforts have been reported in the literature [16–22]. The work in Reference [16] provided a brief illustration of differentiated QoS effect of EDCF function with simulation results. Reference [17] presented a simulation study of IEEE802.11e in the more realistic scenarios. Reference [18] evaluated and compared four QoS support WLAN MAC schemes, including EDCF, using the simulations. References [19,20] presented an adaptive service differentiation scheme called adaptive EDCF. This scheme is derived from EDCF, by incorporating a dynamic CW algorithm, which took into account both application requirements and network conditions. The performances of EDCF and AEDCF algorithms were simulated and compared with prioritized traffic using simulation. Reference [21] proposed to enhance EDCF with a dynamic traffic class management protocols and provided a sliding QoS differentiation mechanism among traffic classes to cope with the instantaneous channel fluctuations. However, little mathematical analysis on EDCF has been reported, partially because it is a very challenging task. Reference [22] derived an analytical model for the throughput performance of an 802.11e Wireless LAN under the EDCF, and proposed an admission control and parameter configuration algorithm that provides the committed throughput guarantees and accepts as many requests as possible. However, the model failed to consider the mutual impact of traffic flows of different classes.

EDCF operation is a complex and high-dynamic process; the performance is affected by a number of factors. Intuitively, the smaller AIFS is, the shorter the waiting period encountered before a VS accessing to the medium. Thus the VS obtains the higher priority when contending for the WM. And this is the same as what the smaller CW does. However, AIFSs differentiation results in more complicated effect in term of the degree of differentiation, which not only depends on the length of AIFSs, but also relies on the combination of AIFS and CW. In this paper, we consider the combined impact of AIFSs and CW related parameters and provide quantitative analysis of QoS supported by EDCF in terms of Saturation Throughput (ST)<sup>||</sup> and access delay by means of a multi-dimensional Markov model. We derive formulas to compute the systems ST, ST ratios and access delay of different flows as function of AIFS and CW parameters. We validate our theoretical analysis by comparing with simulation results. These lead to an accurate evaluation of differentiated QoS provided by IEEE802.11e EDCF as well as the analysis of the impacts of the prioritized parameters on QoS differentiation. Based on these results, we obtain guidelines for the prediction of how the prioritized VSs perform with specific parameters, as well as how to tune the parameters to achieve the desired QoS objectives.

<sup>||</sup>Saturation throughput is defined as the limit reached by the system throughput as the offered load increases till the maximum load that the system can carry in stable conditions. This concept is also interpreted in Reference [14].

### 3. ANALYTICAL MODEL

We focus on the differentiated QoS provided by the IEEE802.11e EDCF under overload conditions. Indeed, the major contributions of this paper are the analytical derivation of system ST, throughput and access delay of individual flows, and the accurate calculation of throughput ratios among flows. The analytical results describe the pattern in which prioritized flows share. More importantly, the calculation of throughput ratios leads to quantitative understanding of to what degree High-Priority (HP) flows can have an advantage over Low-Priority (LP) ones when contending for the WM. Therefore, we gain insight on how well 802.11e EDCF can actually support differentiated QoS using VSs with different AIFS lengths and CW related parameters.

The rest of this section consists of three parts. First, we present and discuss the necessary assumptions used in our analysis. Then, we present an  $m$ -dimensional Markov chain model, and define the state space as well as the transition matrix. Last, according to the theorem of transient states and time to absorption [23, 24], we derive formulation of throughput, throughput ratios among different flows, and the access delay as functions of AIFS lengths and the CW size.

#### 3.1. Model assumptions

A wireless LAN executing EDCF function is a complex system. The performance is influenced by many factors [25]. It is very difficult to take every factor into account at the same time. We make a few necessary assumptions in order to simplify the modelling of system without losing the major operational characteristics of the system.

First, in this paper, we study the EDCF performance in single-hop wireless LANs. We assume the network is fully connected, i.e. every node in the system can hear all other nodes directly. In this case, hidden and exposed terminals would not arise.

Second, we assume ideal channel condition. We ignore the packet loss due to interference of all kinds or capture effects. Thus only packet loss due to packet collision is considered. Packet collision happens when more than one node transmits at the same time.

Third, we analyse EDCF performance when the system operates under saturation conditions, i.e. each VS always has a packet available for transmission; in other words, the transmission queues of the station are always non-empty. While this is not always the case in practice, we should note that the 'ST' is a fundamental performance metric defined as the limit reached by the system throughput as the offered load increases, and represents the maximum load that the system can carry in stable conditions. Similar to other random access schemes, CSMA/CA access methods exhibit a non-linearity in term of throughput change when the traffic load increase to a certain degree. Reference [26] has illustrated and discussed this characteristic of DCF. As the offered load increases, the throughput grows up to a maximum value, referred to as maximum throughput. However, further increase of the offered load leads to a decrease in the system throughput. This results in the practical impossibility to operate DCF function at its maximum throughput for a 'long' period of time. ST indicates the throughput lower bound when the network is running under high load. As well, the access delay derived in saturation condition gives the upper bound for average packet service time. The access delay refers to the time interval between a packet becoming Head of Line (HOL) and its being transmitted successfully, less the time used for the successful data exchange procedure. The bound can be used to predict the performance of a WLAN system.

To evaluate the effect of differentiated AIFS lengths, we set the persistence factor to be one for all virtual stations, which means the CW value will keep constant when collision happens. We justify this assumption by two results: (a) one is valid value for persistent factor according to IEEE802.11 standards [1]. (b) Persistence factor takes effect only when collision occurs, and CW is reset to  $CW_{\min}$  after a successful transmission. We argue that collision is a relatively rare occurrence during the operation of the system when the nodes use EDCF function, which will be illustrated when we discuss the numerical results. We will discuss further how this assumption affects the results in Section 5.

Our last assumption is that the network consists of finite number of nodes. Each node operates only one virtual station. In other words, we ignore the effect of internal virtual collision within a station. This assumption would not take favourable effects on throughput and delay bounds, since internal virtual collision is dealt in a way that the physical collision is avoided, and physical collision results in resource waste.

### 3.2. Multi-dimensional Markov chain model

As shown in Figure 1, in EDCF, the channel would be in one of three states: idle, successful transmission, and collision. The system is in the idle state when all nodes either have no packet to transmit or are executing the sensing and backoff procedure before the data transmission. The system is in the successful transmission state when one and only one node is transmitting a packet without collision. Specifically, it denotes a time interval from sending RTS frame to receiving ACK frame in RTS/CTS mode or a time interval from sending DATA frame to receiving ACK frame in basic transmission mode. The system is in collision state if more than one node tries to exchange packets at the same time. In particular, it denotes a time interval from sending RTS frame to CTS timeout at the sender in RTS/CTS mode or the time sending DATA frame to ACK timeout in basic transmission mode. Three states interleave one another on the time axis. The system throughput is the percentage of successful transmitted payload\*\* over the total time.

Consider a fixed number ( $m$ ) of flows ( $f_1, f_2, \dots, f_m$ ), each of which employs one virtual station equipped with a set of TC-specific parameters, i.e.  $AIFS_i$ ,  $CW_{\min_i}$ ,  $CW_{\max_i}$ , and  $PF_i$  where  $i = 1, 2, \dots, m$ . The difference between any two AIFSs is non-negative integer multiple of a slot time  $\sigma$ .

In our derivation, a discrete and slotted time scale is adopted. Let  $t_n$  denote the time of end of  $n$ th transmission attempt of the system. As illustrated in Figure 1,  $t_0, t_1, t_2 \dots$  represent such time points. The state of the stochastic process at time  $t_n$  is a vector of backoff counters of  $m$  VSs  $B(n) = (b_n^{(1)}, b_n^{(2)}, \dots, b_n^{(m)})$ , where  $b_n^{(i)}$  is the value of backoff counter of the  $i$ th VS at time  $t_n$ . The transmission could be either a successful one or a collision, hence the duration between two consecutive end of transmission may be different. The state of the system changes as a transmission attempt occurs, and at the end of transmission attempt, new backoff counter(s) of VSs, which just completed the transmission attempt, will be randomly generated. Since the state at time  $t_{n+1}$  only relies on the state at time  $t_n$ , we can model this process as an  $m$ -dimensional discrete time Markov chain. The state space of this Markov chain is all possible combinations of  $(b_n^{(1)}, b_n^{(2)}, \dots, b_n^{(m)})$ , where  $b_n^{(i)}$  is any integer between  $[1, CW_i + 1]$ ,  $i = 1, 2, \dots, m$ .

\*\* In this paper, the payload length is normalized by transmission rate.

For convenience and without losing generality, we use a non-negative integer to represent the AIFS length, for example, if  $\text{AIFS} = k$ , it means the length of AIFS is the length of DCF InterFrame Space (DIFS) plus  $k$  slot times ( $\sigma$ ) [1]. According to the 802.11e draft,  $k$  is chosen in the range  $[0, 8]$ .

We next derive the one-step transition matrix  $P$  of the model. From time  $t_n$ , each node starts or resumes the carrier sensing and backoff procedure in order to initiate a packet exchange. Then some nodes will finish their backoff procedure earlier than others and proceed with data transmission. No matter whether the attempt succeeds or fails, in the end, system reaches the time point  $t_{n+1}$ . It is obvious that within the duration  $[t_n, t_{n+1}]$ , there is at least one VS, say  $\text{VS}_j$ , whose backoff counter reaches zero and incurs its transmission attempt, i.e.  $\text{VS}_j$  satisfies  $(b_n^{(j)} + \text{AIFS}_j) = \min_{i \in (1, 2, \dots, m)} (b_n^{(i)} + \text{AIFS}_i)$ . (Note there could be more than one of such  $j$ -like VS satisfying the above minimum condition.) To ease the description of the model, we denote  $s$ ,  $s \in (1, 2, \dots, m)$  as the number of those VSs who execute the  $(n+1)$ st transmission attempt in  $[t_n, t_{n+1}]$ , then  $\text{VS}_{j_1}, \text{VS}_{j_2}, \dots, \text{VS}_{j_s}$  are those  $j$ -like VSs that have to reset their backoff counters by randomly drawing an integer between  $[1, \text{CW}_{j_r} + 1]$ , ( $r = 1, 2, \dots, s$ ) at time  $t_{n+1}$ . Moreover, with the different values of  $s$ , we can distinguish the transmission status into three mutual exclusive and exhaustive groups:

- Group 1: successful transmission (when  $s = 1$ ).
- Group 2: partial collision (when  $1 < s < m$ ).
- Group 3: full collision (when  $s = m$ ).

Hence the state of this Markov chain at time  $t_{n+1}$  becomes  $B(n+1) = (b_{n+1}^{(1)}, b_{n+1}^{(2)}, \dots, b_{n+1}^{(m)})$ , where  $b_{n+1}^{(r)}$  is any integer chosen from  $[1, \text{CW}_{j_r} + 1]$  with uniform distribution,  $r = 1, 2, \dots, s$ .

While those VSs whose backoff counters did not count down to zero within  $[t_n, t_{n+1}]$ , will have their states at  $t_{n+1}$  as:

$$b_{n+1}^{(l)} (l \neq j_1, j_2, \dots, j_s) = \begin{cases} b_n^{(l)} & \text{if } \text{AIFS}_l \geq \text{AIFS}_{j_r} + b_n^{(j_r)} \\ b_n^{(l)} + \text{AIFS}_l - (\text{AIFS}_{j_r} + b_n^{(j_r)}), & \text{AIFS}_l < \text{AIFS}_{j_r} + b_n^{(j_r)} \end{cases}$$

And the one-step transition probability  $P_{B(n) \rightarrow B(n+1)}$  is:

$$[(\text{CW}_{j_1} + 1) \cdot (\text{CW}_{j_2} + 1) \cdots (\text{CW}_{j_s} + 1)]^{-1}$$

Figure 2 illustrates the one-step transition diagram for the collision transmission situation.

### 3.3. Performance analysis

The model can be regarded as a regenerative process. Starting from any full collision state, the system will eventually visit another full collision state; after that, the system will start over a probabilistic replica of the whole process, which ends with another full collision. We define the time interval between two full collision states as a round. Therefore, full collision states of this model are regenerative states and they are identical in that they restart probabilistically identical operation round. The theory of regenerative processes indicates the statistical characteristic in one round is identical to the long-run properties of the system. The following analysis and derivation is based on one round of operation.

Specifically, we define the start of each round as leaving a regenerative state, and ends in the following regenerative state. In other words, a round randomly starts from any valid Markov

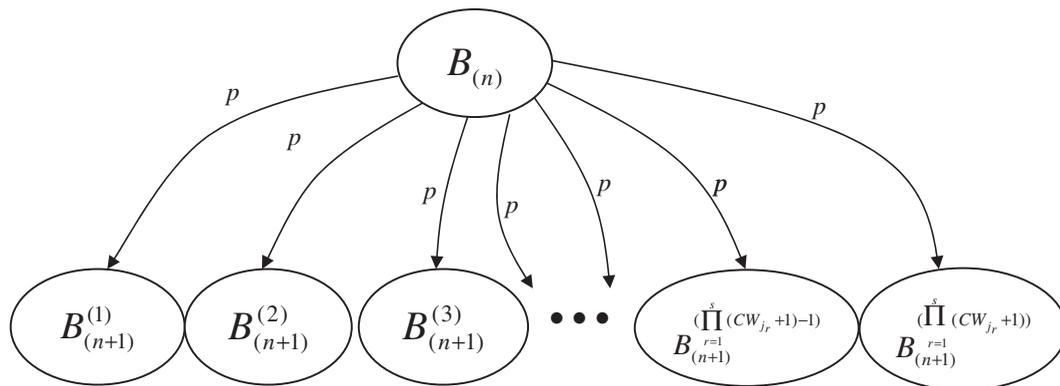


Figure 2. State transition diagram of Markov chain.  $B(n)$  could transit to any of  $[(CW_{j_1} + 1)(CW_{j_2} + 1) \dots (CW_{j_s} + 1)]$  possible states, each with the same probability  $p = 1/[(CW_{j_1} + 1)(CW_{j_2} + 1) \dots (CW_{j_s} + 1)]$ .

state after the last full collision. In order to compute the *throughput and access delay*, we adopt the theorem of *transient state and time to absorption* (refer to References [23, 24]). In one round of operation, the regenerative state, i.e.  $B(n)$  with the property  $b_n^{(1)} + \text{AIFS}_1 = b_n^{(2)} + \text{AIFS}_2 = \dots = b_n^{(m)} + \text{AIFS}_m$  can be taken as an absorbing state, in which case, all VSs are going to send their packets simultaneously within  $[t_n, t_{n+1}]$  and reset their backoff counters at  $t_{n+1}$  consequently. The other states, including both successful and partial collision states, are transient states. Using the theorem on *time to absorption*, we can accurately calculate how many times on average the system will go through each transient state (either successful transmission or partial collision) before being absorbed into absorbing states (full collision) starting from the beginning of a round. Note that the system operation will go on with another round, instead of being absorbed in full collision states.

3.3.1. *Notations and procedure.* The computation procedure is as follows:

1. Compose one-step transition matrix  $P$  of the Markov chain; organize its layout so that the absorbing states are ordered before all transient states. Matrix  $P$  would have the form as  $P = \begin{bmatrix} I & Q \\ R & Q \end{bmatrix}$ , where  $I$  is unit matrix,  $R$  consists of transition probabilities from transit states to absorbing states, and  $Q$  represents transition probabilities from transit states to transit states.
2. Calculate the absorption matrix  $W = (I - Q)^{-1}$ . The element of  $W$ , say  $W_{jk}$  represents the average number of times state  $k$  is visited starting from state  $j$ , where  $j$  and  $k$  are both transient states.
3. Calculate the reaching probability matrix  $F = W \cdot R$ . The element of  $F$ , say  $F_{ji}$  represent the probability that the system turns into absorbing state  $i$  starting from transit state  $j$ .

Denote  $G$  to be the set of transient states of the Markov chain corresponding to the matrix  $Q$ , and  $G^C$  is the set of absorbing states. The transient states of the Markov chain can be further divided into  $m + 1$  subsets according to the transmission results (partial collision or successful)

and the transmitter of the successful transmission. Let  $G_f, G_1, G_2, \dots, G_m$  denote those sets of states, where  $G_f$  is the set of states that results in a partial collision attempt, and  $G_i$  is the set of states that leads to a successful transmission from the  $VS_i$ ,  $i \in (1, 2, \dots, m)$ .

**3.3.2. The system throughput.** We will calculate the *normalized throughput*, defined as the fraction of time when the channel is used to successfully transmit effective payload bits. To do so, we assume the system can equally likely start to operate from any one of valid states. Hence the total throughput of the system  $S$  can be expressed as,

$$S = \frac{E[PL]}{E[T_{\text{round}}]} = \frac{E[\text{successfully trans time}]}{E[\text{success trans time}] + E[\text{collision time}] + E[\text{idle time}]} \quad (1)$$

where  $E[PL]$  is the average successfully transmitted payload (normalized by the channel rate) during one round, it comprises successfully transmitted payload by all VSs. Let  $E[PL_i]$  denote payload transmitted by  $VS_i$ .  $E[PL]$  can be expressed as:

$$E[PL] = \sum_{i \in (1, 2, \dots, m)} E[PL_i] \quad (2)$$

Since there could be more than one transient states (states belonging to set  $G_i$ ) leading to a successful transmission by  $VS_i$ , so the effective payload transmitted by  $VS_i$  is the sum of transmissions from all states of  $G_i$ .  $W_{jk}$  ( $j \in G, k \in G_i$ ) is the average time that the system stays in state  $k$  (leading to a successful transmission by  $VS_i$ ) starting from state  $j$ . Here we assume one system round starts from any valid state of the whole state space  $S$  equally likely, which corresponds to the fact that backoff counter value of any VS is chosen randomly based on its own CW. Since the total number of states is  $|P|$ , i.e. the size of one step transition matrix, we can express the effective payload contributed by  $VS_i$  as:

$$\begin{aligned} E[PL_i] &= E[PL_i | \text{starting from absorbing states}] \cdot P\{\text{starting from absorbing states}\} \\ &+ E[PL_i | \text{starting from transient states}] \cdot P\{\text{starting from transient states}\} \\ &= 0 + \left( E[P_i] \cdot \sum_{j \in G} \sum_{k \in G_i} \frac{W_{jk}}{|W|} \right) \frac{|W|}{|P|} = \frac{1}{|P|} \cdot E[P_i] \cdot \sum_{j \in G} \sum_{k \in G_i} W_{jk} \end{aligned} \quad (3)$$

where  $E[P_i]$  is the normalized average length of packets transmitted by a  $VS_i$  and  $|P|$  is the size of one-step transition probability matrix  $P$ .

In (1),  $E[\text{success trans time}]$  and  $E[\text{collision time}]$  refer to the average channel busy time due to successful transmission and collision, respectively. As per IEEE802.11 specification, two access mechanisms are described, namely, the basic access mechanism and RTS-CTS exchange access mechanism. The two access mechanisms would have different transmission time and collision time. In our research, we will only discuss the RTS-CTS exchange mechanism, since it provides a better performance in the presence of high contention [26].

With RTS-CTS exchange, as shown in Figure 1, we can obtain the channel busy time needed for a successful transmission by the  $i$ th VS ( $T_s^i$ ) and the channel busy time due to

collision ( $T_c$ ) as:

$$\begin{aligned} T_s^i &= \text{RTS} + \text{SIFS} + \delta + \text{CTS} + \text{SIFS} + \delta + H + E[P_i] + \text{SIFS} + \delta + \text{ACK} + \delta \\ T_c &= \text{RTS} + \delta \end{aligned} \quad (4)$$

where  $H = \text{PHY}_{\text{hdr}} + \text{MAC}_{\text{hdr}}$  is the packet header and  $\delta$  is the propagation delay. Similar to the calculation of the effective payload, the time spent on successful transmission consists of all successful transmission by all VSs, which can be expressed as (we shorten success trans time as STT):

$$\begin{aligned} E[\text{STT}] &= E[\text{STT} \mid \text{starting from absorbing states}] \cdot P\{\text{starting from absorbing states}\} \\ &\quad + E[\text{STT}_i \mid \text{starting from transient states}] \cdot P\{\text{starting from transient states}\} \\ &= 0 + \sum_{i \in \{1, 2, \dots, m\}} \sum_{j \in G_i} \sum_{k \in G_i} \left( \frac{W_{jk}}{|W|} \cdot T_s^i \right) \cdot \frac{|W|}{|P|} \\ &= \frac{1}{|P|} \cdot \sum_{i \in \{1, 2, \dots, m\}} T_s^i \cdot \left( \sum_{j \in G_i} \sum_{k \in G_i} W_{jk} \right) \end{aligned} \quad (5)$$

The average channel busy time due to collisions consists of two parts. The first part is attributed to partial collisions before absorption, and its length is equal to the product of the time length of each collision and the sum of the total numbers of partial collision in each round. The second part is the time length of collision attributed to the absorbing state (a full collision). The average channel busy time can be expressed as:

$$\begin{aligned} E[\text{collision time}] &= E[\text{length of all partial collisions}] + E[\text{length of all full collision}] \\ &= E[\text{number of partial collisions}] \cdot E[\text{length of collision}] \\ &\quad + E[\text{number of full collisions}] \cdot E[\text{length of collision}] \\ &= \left( \sum_{j \in G_i} \sum_{k \in G_j} \frac{W_{jk}}{|W|} \cdot \frac{|W|}{|P|} \right) \cdot T_c + 1 \cdot T_c \\ &= \left( \frac{1}{|P|} \cdot \sum_{j \in G_i} \sum_{k \in G_j} W_{jk} + 1 \right) \cdot T_c \end{aligned} \quad (6)$$

The channel will be idle while all VSs are sensing and waiting for free channel. Therefore, all the three types of transmission: successful, partial collision and full collision contribute to the idle time.

Given any state at time  $t_n$ ,  $B(n) = (b_n^{(1)}, b_n^{(2)}, \dots, b_n^{(m)})$ , let  $j_1, j_2, \dots, j_s, 1 \leq s \leq m$  be the VSs having their backoff counters count down to zero and sending packets simultaneously within  $[t_n, t_{n+1}]$ . Let  $I_n$  denote the total idle time before the transmission within  $[t_n, t_{n+1}]$ , then  $I_n$  consists of two consecutive parts, namely, AIFS and idle time due to backoff counter counting down, so we can calculate it as  $I_n = \text{AIFS}_{j_r} + b_n^{j_r}, r \in (1, 2, \dots, s)$ . The average idle time can be

divided into two parts (we shorten idle time as IT):

$$\begin{aligned}
 E[IT] &= \sum_{i \in G^c} E[IT \mid \text{starting from absorbing state } i] \cdot P\{\text{starting from absorbing state } i\} \\
 &\quad + \sum_{j \in G} E[IT \mid \text{starting from transient state } j] \cdot P\{\text{starting from transient state } j\} \\
 &= \frac{1}{|P|} \cdot \sum_{l \in G^c} I_l + \left[ \sum_{j \in G, k \in G} (W_{jk} \cdot I_k) + \sum_{j \in G} \sum_{l \in G^c} (F_{jl} \cdot I_l) \right] \cdot \frac{1}{|P|}
 \end{aligned} \tag{7}$$

Plugging (2), (3), (5), (6), (7) in Equation (1), we then get the system throughput as:

$$S = \frac{\sum_{i \in \{1, 2, \dots, m\}} \sum_{j \in G, k \in G_i} (W_{jk} \cdot E[P_i])}{\sum_{i \in \{1, 2, \dots, m\}} \sum_{j \in G, k \in G_i} (W_{jk} \cdot T_i) + \left( \sum_{j \in G, k \in G_f} (W_{jk} \cdot T_c) + |P| \cdot T_c \right) + \left( \sum_{j \in G, k \in G} (W_{jk} \cdot I_k) + \sum_{l \in G^c} \left( \sum_{j \in G} F_{jl} \right) I_l + \sum_{l \in G^c} I_l \right)} \tag{8}$$

where the denominator is  $|P|$  multiple of the expectation of a round time, i.e.  $|P| \cdot E[T_{\text{round}}]$ .

**3.3.3. Throughput ratios among flows.** Now we can calculate the throughput ratios among the different flows. The effective payload sent by the  $i$ th VS,  $i \in (1, 2, \dots, m)$ , equals to the product of average successful transmission times and average packet length. So the throughput of the  $i$ th VS can be expressed by

$$S_i = \frac{E[PL_i]}{E[T_{\text{round}}]} = \frac{1/|P| \cdot E[P_i] \cdot \sum_{j \in G, k \in G_i} W_{jk}}{E[T_{\text{round}}]} \tag{9}$$

Therefore, the throughput ratios  $S_1 : S_2 : \dots : S_m$  among VSs can be calculated as:

$$\begin{aligned}
 S_1 : S_2 : \dots : S_m &= \left( E[P_1] \cdot \sum_{j \in G, k \in G_1} W_{jk} \right) : \left( E[P_2] \cdot \sum_{j \in G, k \in G_2} W_{jk} \right) \\
 &\dots : \left( E[P_m] \cdot \sum_{j \in G, k \in G_m} W_{jk} \right)
 \end{aligned} \tag{10}$$

and the throughput ratios between any two VSs,  $u, v$ , can be expressed by

$$S_u : S_v = \left( E[P_u] \cdot \sum_{j \in G, k \in G_u} W_{jk} \right) : \left( E[P_v] \cdot \sum_{j \in G, k \in G_v} W_{jk} \right) \tag{11}$$

**3.3.4. Access delay.** We define the access delay as the time between a packet becoming HOL and the starting time of its successful transmission attempt, which is confirmed by ACK control frame (Figure 1, interval between  $t_0$  and  $t_3$ , for a packet in virtual station B). The access delay is also a critical measurement to evaluate QoS in wireless networks [15]. Based on our analytical model, we can compute the average access delay for a packet of individual flows. Specifically, using the concept of  $T_{\text{round}}$ , the average access delay of the packets from the  $i$ th flow,  $T_Q^i$ , is the total waiting time of the  $i$ th flow divided by the total number of the successful transmission by the same flow. The total waiting time of  $i$ th flow, which includes all the time spent for sensing

the channel idle, retransmission time due to collisions, as well as the successful transmission time by other flows, can also be interpreted as the average  $T_{\text{round}}$  less the total time for successful transmission of the  $i$ th VS within one round.

Following the derivation of (3), (4), (5) and (8), we obtain the average access delay of the  $i$ th VS,  $T_Q^i$ :

$$E[T_Q^i] = \frac{E[T_{\text{round}}] - E[T_{\text{success}}^i]}{E[N_s^i]} = \frac{|P| \cdot E[T_{\text{round}}] - T_s^i \cdot \sum_{j \in G} \sum_{k \in G_i} W_{jk}}{\sum_{j \in G} \sum_{k \in G_i} W_{jk}} \quad (12)$$

where  $E[T_{\text{success}}^i]$  is the average time of a successful transmission for the  $i$ th VS, and  $E[N_s^i]$  is the average number of successful transmissions by the  $i$ th VS.

#### 4. NUMERICAL RESULTS AND ANALYTICAL MODEL VALIDATION

In order to validate our analytical model, we compare it with a simulation model. Numerical results from the analytical model are obtained using MATLAB. Our simulations are written in C++ . In the simulations, all stations operate independently in the RTS/CTS mode under the MAC protocol conforming to the specifications in Reference [1]. A summary of the constant parameter values used in both analytical model and simulation model are given in Table I (refer to Reference [27], 15.3.3 DS PHY characteristics). For simplicity, we set the same constant payload size for the packets from all flows.

We designed the first experiment scenario, which consists of two flows of different TCs. Both flows use the same CW values, i.e.  $CW_{\text{HP}} = CW_{\text{LP}} = 7$ .  $AIFS_{\text{HP}}$  is fixed at 0,  $AIFS_{\text{LP}}$  increments from 0 to 8. Table II presents a numerical comparison of throughput and throughput ratios obtained from analytical model (depicted by MAT) and simulation (depicted by SIM). Simulation results in all scenarios have a 95% confidence level with 5% confidence intervals. The comparison illustrates that difference between the two models are negligible, and that our analytical model is, indeed, accurate. Moreover, all the results reported in Figures 3–9 have also been compared with simulation results, with negligible differences observed.

Table I. Constant parameters in analytical model and simulations.

Packet payload size (bits)	8196
PHY header (bits)	192
MAC header (bits)	272
RTS (bits)	160
CTS (bits)	112
ACK (bits)	112
WM transmission rate (bits/s)	11M
Propagation delay ( $\mu\text{s}$ )	1
SIFS ( $\mu\text{s}$ )	10
Slot time $\sigma$ ( $\mu\text{s}$ )	20
PIFS = SIFS + $\sigma$ ( $\mu\text{s}$ )	30
DIFS = SIFS + $2\sigma$ ( $\mu\text{s}$ )	50

Table II. Comparison of analytical and simulation results.

AIFS <sub>LP</sub> - AIFS <sub>HP</sub>	S		HP throughput		LP throughput		Ratio	
	S-MAT	S-SIM	HP-MAT	HP-SIM	LP-MAT	LP-SIM	HP: LP MAT	HP : LP SIM
0	0.759	0.740	0.379	0.371	0.379	0.369	1.000	1.004
1	0.753	0.735	0.471	0.460	0.283	0.275	1.665	1.669
2	0.749	0.731	0.542	0.530	0.207	0.201	2.626	2.634
3	0.745	0.729	0.598	0.585	0.147	0.144	4.071	4.058
4	0.742	0.726	0.644	0.630	0.099	0.096	6.526	6.561
5	0.739	0.724	0.684	0.670	0.055	0.054	12.393	12.365
6	0.737	0.723	0.717	0.704	0.020	0.020	35.352	35.644
7	0.735	0.724	0.735	0.724	0.000	0.000	Inf	Inf

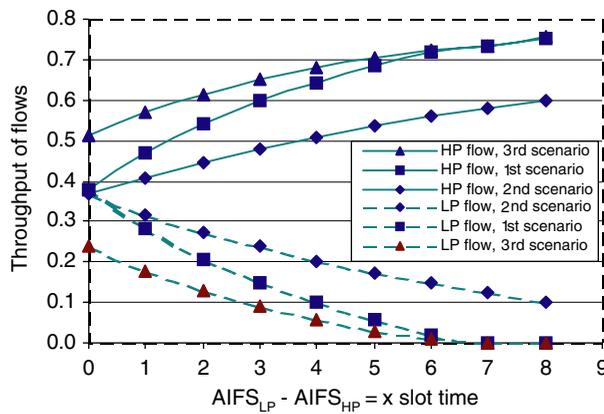


Figure 3. Throughput ratio vs AIFS difference.

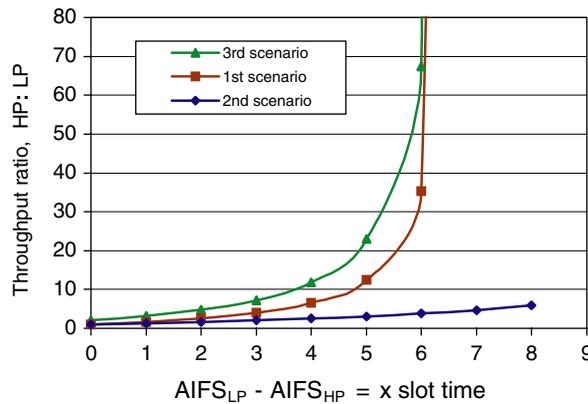


Figure 4. Throughput ratio vs AIFS difference.

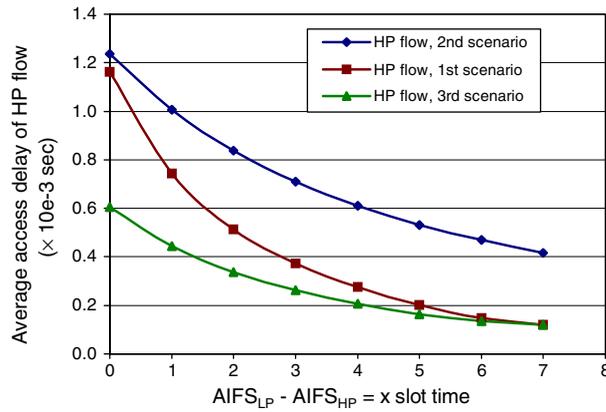


Figure 5. Access delay of HP flow vs AIFS difference.

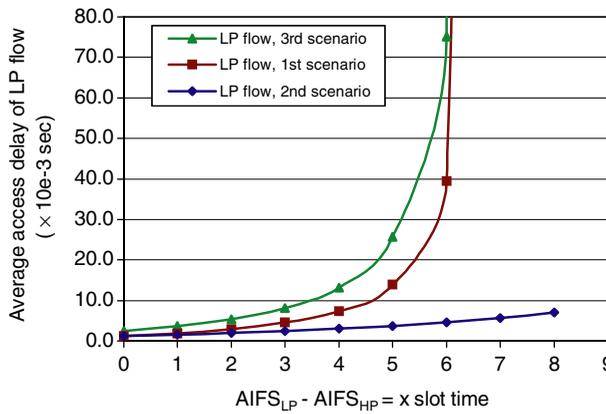


Figure 6. Access delay of LP flow vs AIFS difference.

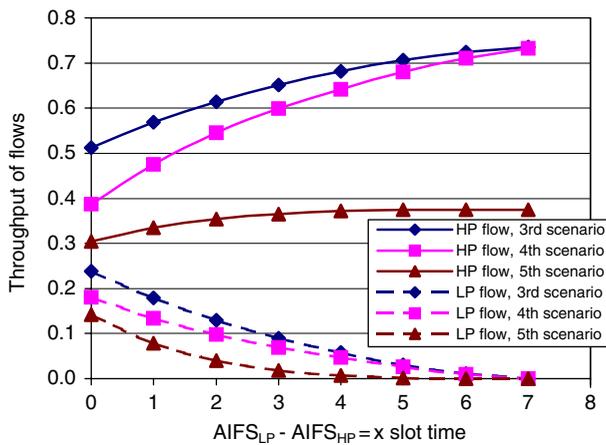


Figure 7. Impact of traffic load on flow throughput ratio.

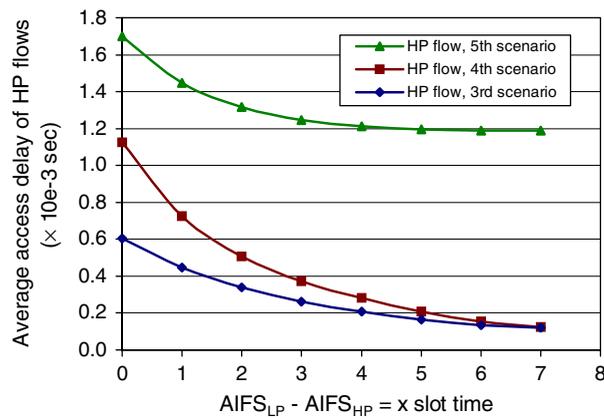


Figure 8. Impact of traffic load on access delay of HP flow.

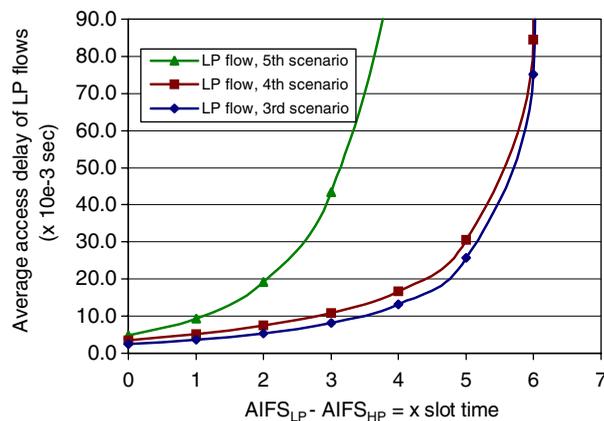


Figure 9. Impact of traffic load on access delay of LP flow.

## 5. PERFORMANCE EVALUATION

In this section, we investigate the performance of differentiated QoS supported by the 802.11e EDCF MAC scheme. The metrics include throughput of the system, throughput and access delay of individual flows, and throughput ratio among flows. The throughput and access delay of individual flows indicates how the flows are served distinctively as a result of TC-specific prioritized parameters, while the throughput ratio reflects quantitatively the QoS differentiation, i.e. to what degree, the HP TCs have an advantage over LP ones.

### 5.1. The compound effect of AIFS And CW on QoS

To explore the comprehensive impact of differentiated AIFSs and CWs, we design another two sets of experiments. The second scenario consists of two flows and each flow has the same

parameters as the above experiments, except that both flows use  $CW = 15$ ; and the LP flow increases AIFS length by one slot time each time. The third scenario also consists of two flows. However, the HP flow has  $CW_{HP} = 7$ , the LP flow has  $CW_{LP} = 15$ ; i.e. both AIFSs and CWs are differentiated.

Figure 3 illustrates throughput of the HP flow and the LP flow of the three sets of experiments. Figure 4 shows the throughput ratios between the HP and LP flows in each scenario. Figures 5 and 6, respectively, show access delay of the HP flow and LP flow of the experiments.

We make the following observations. First, we note that the smaller the CWs are, the more significant the influence of AIFS on QoS differentiation will be. Secondly, the combination of differentiated AIFSs and differentiated CWs introduce more compound and significant effect on the degree of differentiation. Obviously, scenario three shows a more intensive differentiation in term of both throughput and access delay with the increase of AIFS difference. Moreover, we argue that it is the AIFS difference, rather than the absolute AIFS values, that determines the degree of QoS differentiation. As displayed in Figure 4, the increment of throughput ratio accelerates with the growth of AIFSs difference non-linearly. The larger the AIFSs difference, the faster the ratio increases, and in the worst case, the LP flow may completely lose the opportunity to access medium.

### 5.2. Effect of traffic loading on QoS

Here we evaluate the performance as the traffic load changes. Figures 7, 8 and 9, respectively, show the results of the throughput of HP flow and LP flow, access delay of HP flow, and access delay of LP flow. Each HP flow adopts the TC-specific parameters as  $CW_{HP} = 7$  and  $AIFS_{HP} = 0$ ; Each LP flow has TC-specific parameters as  $CW_{LP} = 15$  and  $AIFS_{LP}$  is incremented from 0 to 7 as the experiment proceeds. Each figure plots the following cases: (a) scenario three: one HP flow and one LP, (b) scenario four: one HP flow and two identical LP flows (c) scenario five: two identical HP flows and one LP flow. From the results we can see that the HP flows can dominate the share of wireless medium and are less affected by LP flows. To our surprise, a small difference in AIFS (one slot time) between two flows can result in considerable large difference of their throughput and access delay when there is one more HP flow.

### 5.3. Discussion

In order to advocate the argument that collisions are relatively infrequent occurrences compared to successful transmissions, we further investigate the experimental results based on the analytical model. Table III summarizes the results of average number of collisions and successful transmissions during one round of operation, in two cases.

Table III. Summary of collisions and transmission attempts.

	Case one—one HP and two LP	Case two—two HP and one LP
Transmission attempts in one round	194.9	196.9
Collisions in one round	16.8	27.3
Ratio of collisions over total transmission	0.094	0.139

The second case is a snapshot of the fourth scenario, consists of one HP flow and two LP flows. The HP flow and the LP flows use the same parameters as above. The ratio of collision over the total transmission attempts is 0.094.

The first case is a snapshot of the fifth scenario, which composes of two HP flows and one LP flow. Both HP flows use the parameters as  $AIFS_{HP} = 0$ , and  $CW_{HP} = 7$ ; while LP flow uses the parameters as  $AIFS_{LP} = 3$  and  $CW_{LP} = 15$ . The ratio of collision over the total transmission attempts is 0.139.

We set PF to one for all experiment—an extreme case. However, since the collisions are infrequent during the operation of system, our results should be representative for other valid PF value cases. Furthermore, since a PF value greater than one might help to reduce the happening of collisions, so the throughput results using PF as one would be the upper bound value in the corresponding experimental cases.

## 6. CONCLUDING REMARKS

In this paper, we developed an accurate multi-dimensional Markov model to analyse the performance of the IEEE 802.11e EDCF MAC protocol. Particularly, the model can be used to evaluate the ability of the IEEE 802.11e EDCF to provide differentiated QoS. Based on the proposed analytical model, we have derived formulations of saturation throughput, throughput ratio of flows and access delay as functions of the prioritized parameters. It also has been used to conduct quantitative analysis of the impact of parameters such as AIFS and CW on the performance of prioritized flows.

Numerical results show that EDCF can well support differentiated QoS, and it provides significant advantage to higher priority flows. Numerical results show that AIFS has a significant impact on the TC priority. Fixing other parameters, the smaller the AIFS is, the higher the priority of a flow, and the shorter time the flow will wait before transmitting. This in turn translates into higher bandwidth share of higher priority flows. Hence, we conclude that the IEEE 802.11 EDCF function can effectively provide QoS differentiation.

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